SCHEME 11

COMPUTER SCIENCE 61A

July 28, 2015

1 Introduction

In the next part of the course, we will be working with the **Scheme** programming language. In addition to learning how to write Scheme programs, we will eventually write a Scheme interpreter in Project 4!

Scheme is a dialect of the **Lisp** programming language, a language dating back to 1958. The popularity of Scheme within the programming language community stems from its simplicity – in fact, previous versions of CS 61A were taught in the Scheme language.

2 Primitives

Scheme has a set of *atomic* primitive expressions. Atomic means that these expressions cannot be divided up.

```
scm> 123
123
scm> 123.123
123.123
scm> #t
True
scm> #f
False
scm> 'a      ; this is a symbol
a
```

To define variables:

```
scm> (define a 3)
a
scm> a
3
```

The `define` statement binds a value to a variable (just like the assignment operator in Python); in addition, `define` returns the variable name (in this case, `a`).

More precisely, `define` returns the *symbol* `a`. As you saw above, when you type `'a`, you also get the symbol `a`. This is because when you use the single quote, you're telling Scheme not to follow the normal rules of evaluation and just have the symbol return as itself.

2.1 Questions

1. What would Scheme print?

```
scm> (define a 1)

scm> a

scm> (define b a)

scm> b

scm> (define c 'a)

scm> c
```

3 Call Expressions

Now, just defining variables and printing out primitives isn't very useful. You want to call functions too:

```
scm> (+ 1 2)
3
scm> (- 2 3)
-1
```

```
scm> (* 6 3)
18
scm> (/ 5 2)
2.5
scm> (+ 1 (* 3 4))
13
```

To call a function in Scheme, you first need a set of parenthses. Inside of the parentheses, you give the symbol for the function name, then you give the arguments (remember the spaces!).

Evaluating a Scheme function call works just like Python:

1. Evaluate the operator (the first expression after the `(`), then evaluate each of the arguments.
2. Apply the operator to those evaluated arguments.

When you evaluate `(+ 1 2)`, you evaluate the `+` symbol which is bound to a built-in addition function, then you evaluate `1` and `2`. Finally, you apply the addition function to `1` and `2`.

Some important functions you'll want to use are:

- `+`, `-`, `*`, `/`
- `eq?`, `=`, `>`, `>=`, `<`, `<=`

3.1 Questions

1. What would Scheme print?

```
scm> (+ 1)


scm> (* 3)


scm> (+ (* 3 3) (* 4 4))


scm> (define a (define b 3))


scm> a


scm> b
```

4 Special Forms

There are certain expressions that look like function calls, but *don't* follow the rule for order of evaluation. These are called *special forms*. You've already seen one — `define`, where the first argument, the variable name, doesn't actually get evaluated to a value.

4.1 If Statements

Another common special form is the **`if`** form. An **`if`** expression looks like:

```
(if <CONDITION> <THEN> <ELSE>)
```

where `<CONDITION>`, `<THEN>` and `<ELSE>` are expressions. First, `<CONDITION>` is evaluated. If it evaluates to `#f`, then `<ELSE>` is evaluated. Otherwise, `<THEN>` is evaluated. Every primitive expression that is not `False` evaluates to "true".

```
scm> (if (< 4 5) 1 2)
1
scm> (if False (/ 1 0) 42)
42
```

4.2 Boolean operators

Boolean operators (**`and`** and **`or`**) are also special forms because they are short-circuiting operators (just like in Python).

```
scm> (and 1 2 3)
3
scm> (or 1 2 3)
1
scm> (or True (/ 1 0))
True
scm> (and False (/1 0))
False
scm> (not 3)
False
scm> (not True)
False
```

4.3 Questions

1. What does Scheme print?

```
scm> (if (or #t (/ 1 0)) 1 (/ 1 0))


scm> (if (> 4 3) (+ 1 2 3 4) (+ 3 4 (* 3 2)))


scm> ((if (< 4 3) + -) 4 100)
```

4.4 Lambdas and Defining Functions

Scheme has lambdas too! The syntax is

```
(lambda (<PARAMETERS>) <EXPR>)
```

Like in Python, lambdas are function values. Also like in Python, when a lambda expression is called in Scheme, a new frame is created where the parameters are bound to the arguments passed in. Then, `<EXPR>` is evaluated under this new frame. Note that `<EXPR>` is not evaluated until the lambda function is called.

```
scm> (define x 3)
x
scm> (define y 4)
y
scm> ((lambda (x y) (+ x y)) 6 7)
13
```

Like in Python, lambda functions are also values! So you can do this to define functions:

```
scm> (define square (lambda (x) (* x x)))
square
scm> (square 4)
16
```

This can be a bit tedious though. Luckily Scheme has a shortcut: our old friend `define`:

```
scm> (define (square x) (* x x))
square
scm> (square 5)
25
```

When you do `(define (<FUNCTION NAME> <PARAMETERS>) <EXPR>)`, Scheme will automatically transform it to `(define <FUNCTION NAME> (lambda (<PARAMETERS>) <EXPR>))`. In this way, lambdas are more central to Scheme than they are to Python.

4.5 Let

There is also a special form based around `lambda`: `let`. The structure of `let` is as follows:

```
(let ( (<SYMBOL1> <EXPR1>)
       ...
       (<SYMBOLN> <EXPRN>) )
      <BODY> )
```

This special form really just gets transformed to:

```
( (lambda (<SYMBOL1> ... <SYMBOLN>) <BODY>) <EXPR1> ... <EXPRN>)
```

`let` effectively just binds symbols to expressions, then runs its body. This can be useful if you need to reuse a value multiple times, or if you want to make your code more readable:

```
(define (sin x)
    (if (< x 0.000001)
        x
        (let ( (recursive-step (sin (/ x 3))) )
            (- (* 3 recursive-step)
               (* 4 (expt recursive-step 3))))))
```

4.6 Questions

1. Write a function that calculates factorial. (Note we have not seen any iteration yet.)

```
(define (factorial x)





                                                )
```

2. Write a function that calculates the n^{th} Fibonacci number.

```
(define (fib n)
    (if (< n 2)
        1



                                                )
```

5 Pairs and Lists

So far, we have lambdas and a few atomic primitives. How do we create larger, more complicated data structures? Well, the most important data structure in Scheme is the **pair**. A pair is an abstract data type with the constructor `cons` (which takes two arguments), and two selectors, `car` and `cdr` (which get the first and second argument respectively). `car` and `cdr` don't stand for anything anymore, but if you want the history go to http://en.wikipedia.org/wiki/CAR_and_CDR.

```
scm> (define a (cons 1 2))
a
scm> a
(1 . 2)
scm> (car a)
1
scm> (cdr a)
2
```

Note that when a `pair` is printed, the `car` and `cdr` elements are separated by a period. Remember, `cons` always takes in exactly two arguments.

A common data structure that you build out of pairs is the list. A list is either the empty list, which is another primitive represented as `'()` or `nil`, or a `cons` pair where the `cdr` is a list. (Note the similarity to `Link`s!)

```
scm> '()
()
scm> nil
()
scm> (cons 1 (cons 2 nil))
(1 2)
scm> (cons 1 (cons 2 (cons 3 nil)))
(1 2 3)
```

Note that there are no dots here. When a dot is followed by a left parenthesis, the dot, left parenthesis, and matching right parenthesis are deleted. You can check if a list is `nil` with the `null?` function.

A shorthand for writing out a list is:

```
scm> '(1 2 3)
(1 2 3)
scm> '(define (square x) (* x x))
(define (square x) (* x x))
```

You might notice that the evaluation of the second expression looks a lot like Scheme code. That's because Scheme code is made up of lists. When you quote an expression (like a list), you're telling Scheme not to evaluate the expression, but instead keep it as is. This is one of the reasons why Scheme is cool – it can be defined within itself!

5.1 Questions

1. Fill in the following to complete an abstract data type for binary trees, in which each node has at most 2 children, `left` and `right`:

```
(define (make-btree entry left right)
    (cons entry (cons left right)))

(define (entry tree)
                        )

(define (left tree)
                        )

(define (right tree)
                        )
```

2. Using the above definition, write a function that sums up the entries of a binary tree, assuming that the entries are all numbers.

```
(define (btree-sum tree)








)
```

3. Define `map`, where the first argument is a function and the second a list. This should work like **Python**'s `map`.

```
(define (map fn lst)







                                                    )
```

4. Define `reduce`, where the first argument is a function that takes two arguments, the second is a starting value, and the third is a list. This should work like **Python**'s `reduce`.

```
(define (reduce fn s lst)



                                                  )
```

6 Extra Questions

1. Write a Scheme function that, when given an element, a list, and a position, inserts the element into the list at that position.

```
(define (insert element lst position)



                                                  )
```

2. Write a Scheme function that, when given a list, such as `(1 2 3 4)`, duplicates every element in the list (i.e. `(1 1 2 2 3 3 4 4)`).

```
(define (duplicate lst)



                                                  )
```